

# Features of Potential Signal of Square-wave Voltammetry to Calculate Voltammograms in MATHCAD

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MATHCAD working file is presented for simulation of theoretical voltammograms of a two-step Surface Mechanism coupled with preceding chemical step.

We show the definition and the features of the SWV signal, and how this potential ramp can be calculated in MATHCAD Software.

## Legends of the symbols used in MATHCAD File:

**potI<sub>j</sub>** and **potII<sub>j</sub>** are symbols for time-dependent potential in SWV  $j$  and  $k$ - are symbols of the magnitude of potential steps applied  $r$  - is a counter parameter

**R** - is universal gas constant

$x$  - is symbol for initiation of calculation of the complex equation for current estimation

$\Delta E$  – is the potential width of

$\alpha_1$  and  $\alpha_2$  – are symbols for the electron transfer coefficients of the first and second electron transfer step, respectively

**E<sub>sI</sub>** and **E<sub>sII</sub>** are the formal redox potentials of the first and the second electron transfer step

**K<sub>I</sub>** and **K<sub>II</sub>** are the dimensionless rate parameters of the first and the second electrode transformation, respectively;

**E<sub>sw</sub>** is the square wave amplitude (50 mV in this file)

**dE** is potential step (10 mV in this file)

**Sk** is a numerical integration factor

**potI<sub>j</sub>** and **potII<sub>j</sub>** are the formulas for the potential ramp in SWV; they are calculated by a common function by considering the parameters that affect the SWV bias, i.e. the **E<sub>sI</sub>**, **E<sub>sII</sub>**, **E<sub>sw</sub>** and **dE**.

$\Phi_{Ij}$  and  $\Phi_{IIj}$  are the dimensionless potentials of the first and the second electron transfer step

$\Psi_{Ij}$  and  $\Psi_{IIj}$  are the total currents of the first and the second electron transfer steps, respectively

$\Psi_{net} = \Psi_{Ij} + \Psi_{IIj}$  is the total current that unifies both electron transfer steps

Meaning of other symbols, and calculating procedure is given in the working file below

$$Esl := 0.2 \quad \Delta E := 0.8 \quad dE := 0.01 \quad Esw := 0.05$$

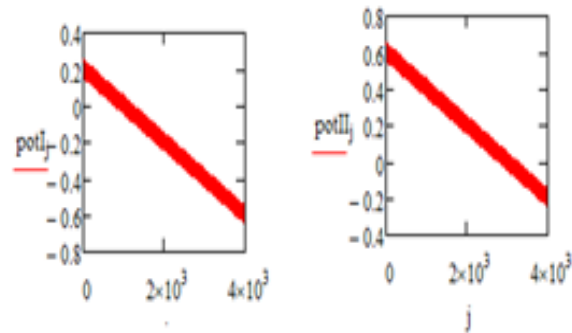
$$n := 1 \quad F := 96500 \quad R := 8.314 \quad T := 298.15$$

$$j := 1.. \frac{\Delta E}{dE} \cdot 50$$

$$\alpha 2 := 0.5$$

$$potI_j := Esl + Esw - \left[ \left( \text{ceil} \left( \frac{j}{25} \cdot \frac{1}{2} \right) \cdot dE + \text{if} \left( \frac{\text{ceil} \left( \frac{j}{25} \right)}{2} = \text{ceil} \left( \frac{j}{25} \cdot \frac{1}{2} \right), 1, -1 \right) \cdot Esw + Esw \right) - dE \right]$$

$$potII_j := EsII + Esw - \left[ \left( \text{ceil} \left( \frac{j}{25} \cdot \frac{1}{2} \right) \cdot dE + \text{if} \left( \frac{\text{ceil} \left( \frac{j}{25} \right)}{2} = \text{ceil} \left( \frac{j}{25} \cdot \frac{1}{2} \right), 1, -1 \right) \cdot Esw + Esw \right) - dE \right]$$



$$\Phi I_j := n \cdot \frac{F}{R \cdot T} \cdot potI_j \quad \Phi II_j := n \cdot \frac{F}{R \cdot T} \cdot potII_j$$

$$x := 0.001$$

$$\Psi I_{1,r} := \text{root} \left[ \frac{\frac{K I_r \cdot e^{-\alpha 1 \cdot \Phi I_1} \cdot K}{1 + K} \cdot \left( 1 - \frac{1}{50} \cdot 0 \right) - (z)^{-1} \cdot K I_r \cdot \left( \frac{1}{1 + K} \right) \cdot (-1) \cdot e^{-\alpha 1 \cdot \Phi I_1 \cdot 0} - \frac{K I_r}{50} \cdot e^{\Phi I_1 \cdot (1 - \alpha 1) \cdot 0}}{\frac{K I_r \cdot e^{-\alpha 1 \cdot \Phi I_1} \cdot K}{1 + K} \cdot \frac{1}{50} + 1 + (z)^{-1} \cdot K I_r \cdot (-1) \cdot \left( \frac{1}{1 + K} \right) \cdot S_1 \cdot e^{-\alpha 1 \cdot \Phi I_1} + \frac{K I_r}{50} \cdot e^{\Phi I_1 \cdot (1 - \alpha 1)}} \cdot (1 + 0) \right] \cdot x - \frac{K I_r}{50} \cdot e^{(1 - \alpha 1) \cdot \Phi I_1} \cdot \left[ \frac{x \cdot \frac{K II \cdot e^{-\alpha 2 \cdot \Phi II_1}}{50}}{1 + \frac{K II \cdot e^{-\alpha 2 \cdot \Phi II_1}}{50} \cdot (1 + e^{\Phi II_1})} \right] - K I_r \cdot e^{-\alpha 2 \cdot \Phi I_1 \cdot x}$$

$$\Psi II_{1,r} := \frac{\Psi I_{1,r} \cdot \frac{K II \cdot e^{-\alpha 2 \cdot \Phi II_1}}{50}}{1 + \frac{K II \cdot e^{-\alpha 2 \cdot \Phi II_1}}{50} \cdot (1 + e^{\Phi II_1})}$$

$$r := 1..1$$

$$EsII := 0.6$$

$$K I_r := 10^{0 \cdot r}$$

$$K II := 10^0$$

$$\alpha 1 := 0.5$$

$$\log(K I_r) =$$

$$0$$

$$K := 0.1$$

$$z := 2$$

$$k := 1.. \frac{\Delta E}{dE} \cdot 50$$

$$S_k := e^{\frac{z}{50} \cdot (-k)} - e^{\frac{z}{50} \cdot (-k+1)}$$

## TWO STEP SURFACE CEE MECHANISM MATHEMATICAL MODEL IN SQUARE WAVE VOLTAMMETRY

KI and KII are kinetic parameters related to the first and second electron transfer step  
alpha is the electron transfer coefficient  
Esl and EsII are potentials related to the first and the second electron transfer step  
n is number of electron exchanged  
F is Faraday constant  
Esw is SWV amplitude  
T is temperature  
dE is potential step  
Phi is dimensionless potential  
Psi is dimensionless current  
K is equilibrium constant -K<sub>eq</sub>  
z is dimensionless chemical parameter -K<sub>chemical</sub> = z/f

$$\vartheta_{1,j}^{\pm}=\max\left\{n-\frac{\Re z}{t},-\alpha\frac{\theta_j^{\pm}}{t}\right\}\cdot\left[\frac{\frac{\Re z}{1-\Re z}\left[1+\frac{1}{2t}\left(1+\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}\right)\right]-\left(\frac{1}{t}\right)^{-1}\cdot\left(\frac{1}{1-\Re z}\right)\cdot(-1)^{\frac{\theta_j^{\pm}}{t}}\cdot\left[1+\sum_{i=1}^{j-1}\left(\vartheta_{1,i}^{\pm}\frac{S_{i-1}}{t}\right)^{-1}\right]-0}{\frac{\Re z}{1-\Re z}\frac{\Re z}{t}e^{-\alpha\frac{\theta_j^{\pm}}{t}}+1+\left(\frac{1}{t}\right)^{-1}\frac{1}{2t}\cdot(-1)^{\frac{\theta_j^{\pm}}{t}}\cdot\left(\frac{1}{1-\Re z}\right)\cdot S_{j-1}e^{-\alpha\frac{\theta_j^{\pm}}{t}}+\Re z\frac{(-1)^{\frac{\theta_j^{\pm}}{t}}}{t}}\right]+\frac{\frac{\theta_j^{\pm}}{t}}{t}\cdot\left[\frac{1}{1+\frac{\theta_j^{\pm}}{t}}\cdot\left(1+\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}\right)\cdot\frac{2t}{\Re z\frac{(-1)^{\frac{\theta_j^{\pm}}{t}}}{t}\cdot\left[1+\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}\right]+\frac{\theta_j^{\pm}}{t}}}\cdot\left[\frac{\Re z}{t}e^{-\alpha\frac{\theta_j^{\pm}}{t}}\cdot\left[1+\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}\right]+\frac{1}{2t}\cdot\left(1+\frac{\theta_j^{\pm}}{t}\right)\right]\cdot\frac{2t}{\Re z\frac{(-1)^{\frac{\theta_j^{\pm}}{t}}}{t}\cdot\left[1+\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}\right]-\left(\frac{1}{t}\right)^{-1}\cdot\left(\frac{1}{1-\Re z}\right)\cdot\left[1+\sum_{i=1}^{j-1}\left(\vartheta_{1,i}^{\pm}\frac{S_{i-1}}{t}\right)^{-1}\right]}\cdot\left[1+\frac{1}{2t}\cdot\left(1+\frac{\theta_j^{\pm}}{t}\right)\right]\cdot\left(\frac{1}{1-\Re z}\right)\cdot\left[1+\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}\frac{S_{i-1}}{t}\right]\right]\right]$$

$$\vartheta_{1,j}^{\pm}=\frac{\Re z}{2+\Re z}\frac{e^{-\alpha\frac{\theta_j^{\pm}}{t}}}{e^{-\alpha\frac{\theta_j^{\pm}}{t}}\cdot\left(1+\frac{\theta_j^{\pm}}{t}\right)}\cdot\sum_{i=1}^j\vartheta_{1,i}^{\pm}+\frac{\Re z}{2+\Re z}\frac{(-1)^{\frac{\theta_j^{\pm}}{t}}\cdot\left(\frac{1}{t}\right)^{-1}\cdot\frac{\theta_j^{\pm}}{t}}{e^{-\alpha\frac{\theta_j^{\pm}}{t}}\cdot\left(1+\frac{\theta_j^{\pm}}{t}\right)}\cdot\sum_{i=1}^{j-1}\vartheta_{1,i}^{\pm}$$

$$\vartheta_{1,j}^{\pm}=\vartheta_{1,j}^{\pm}+\vartheta_{1,j}^{\pm}$$

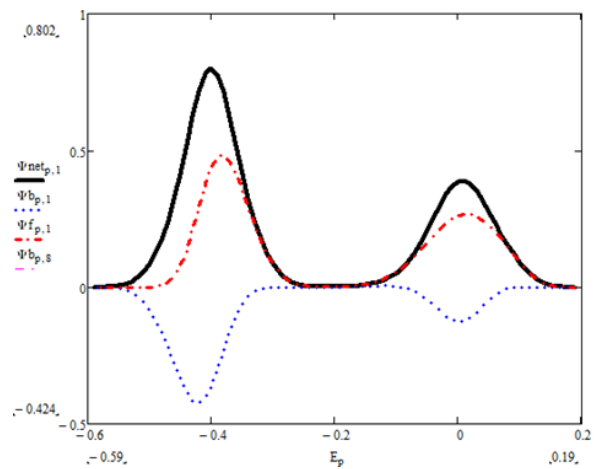
$$t>1\cdot\left(\frac{1}{\Re z}\right)+1$$

$$\vartheta_{1,j}^{\pm}>\vartheta_{1,\frac{p-1}{2}+1,j}^{\pm}\vartheta_{1,j}^{\pm}=\vartheta_{1,\frac{p-1}{2}+1,j}^{\pm}\vartheta_{1,j}^{\pm}>\vartheta_{1,\frac{p-1}{2}}^{\pm}-\vartheta_{1,j}^{\pm}$$

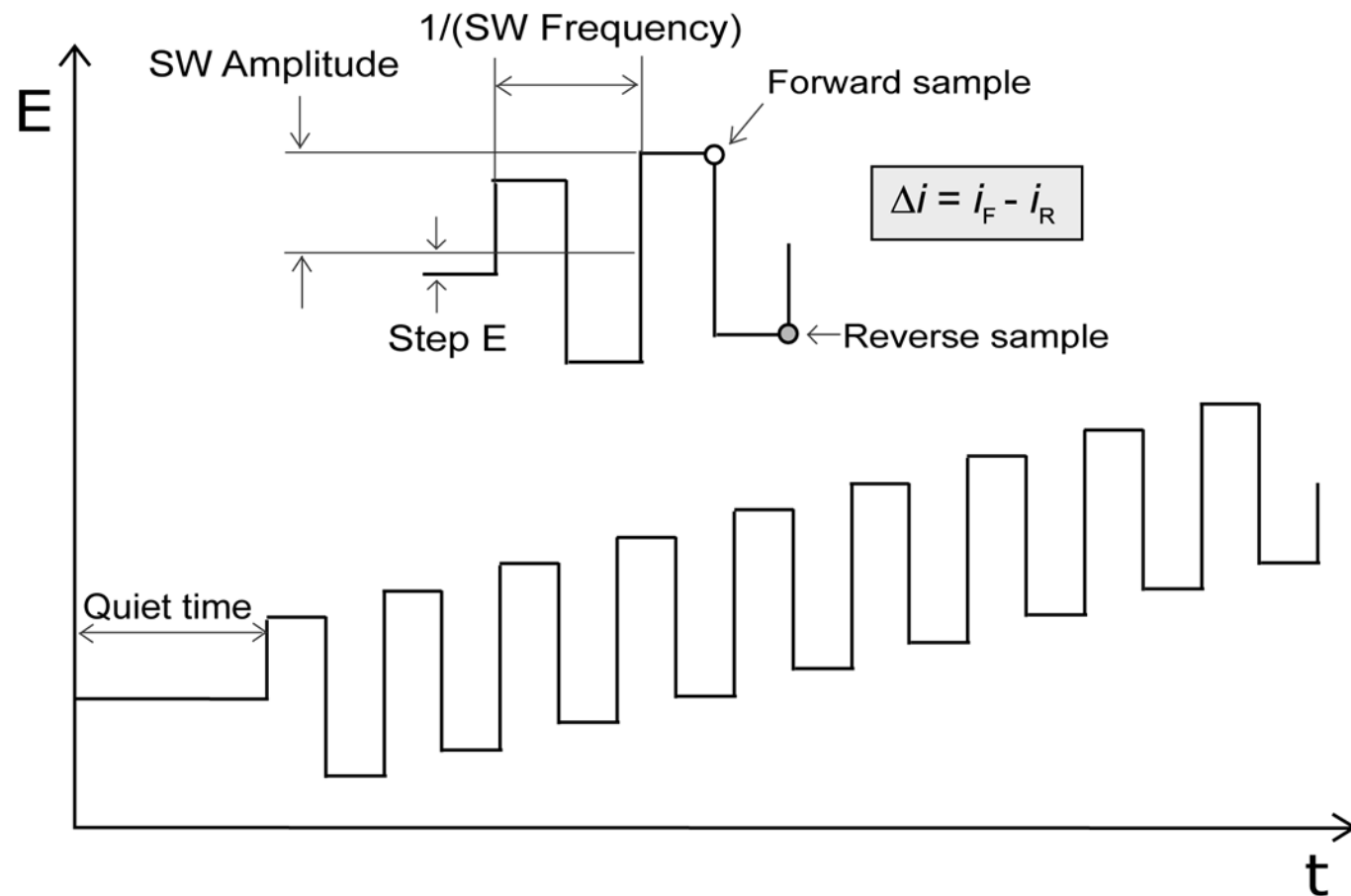
$$\vartheta_{1,j}^{\pm}=\vartheta_{1,\frac{p-1}{2}+1,j}^{\pm}\vartheta_{1,j}^{\pm}=\vartheta_{1,\frac{p-1}{2}+1,j}^{\pm}\vartheta_{1,j}^{\pm}>\vartheta_{1,j}^{\pm}\cdot\vartheta_{1,j}^{\pm}$$

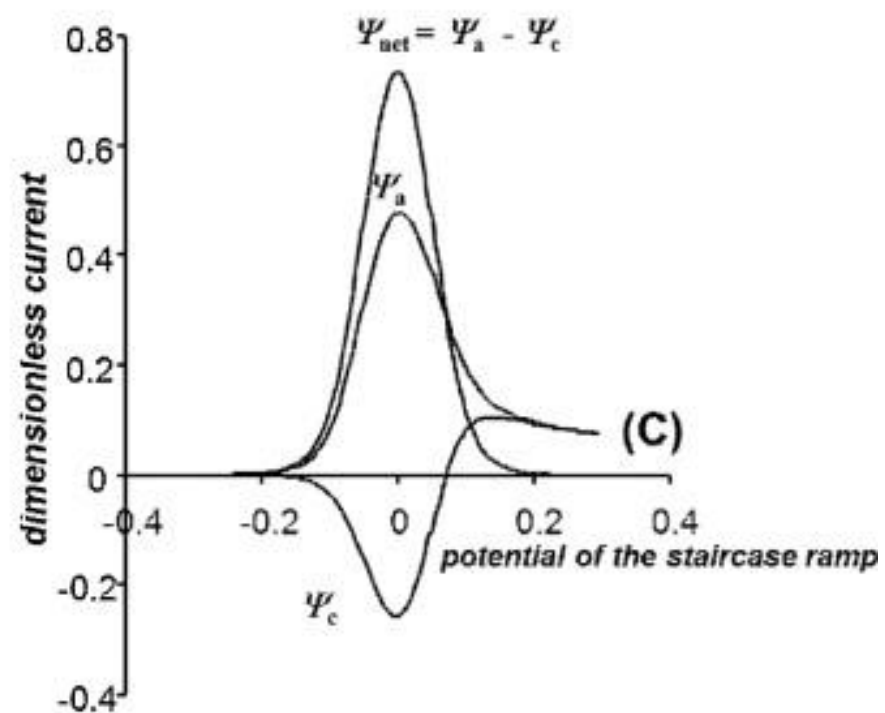
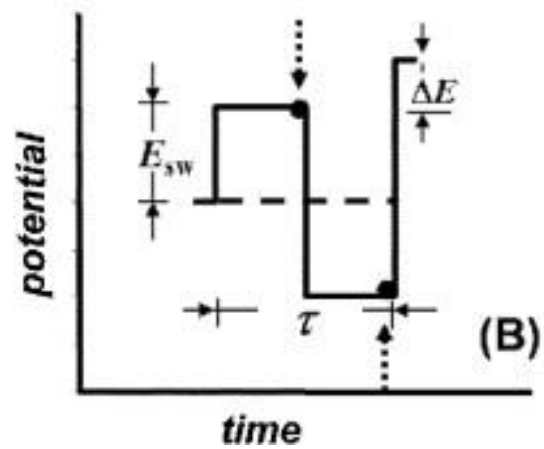
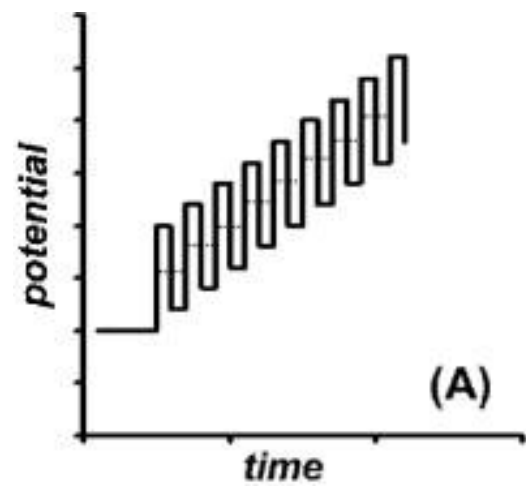
$$\vartheta_{1,j}^{\pm}>\vartheta_{1,\frac{p-1}{2}+1,j}^{\pm}\vartheta_{1,j}^{\pm}=\vartheta_{1,\frac{p-1}{2}+1,j}^{\pm}\vartheta_{1,j}^{\pm}=\vartheta_{1,\frac{p-1}{2}}^{\pm}\cdot\vartheta_{1,j}^{\pm}$$

$$\vartheta_{1,j}^{\pm}=\vartheta_{1,j}^{\pm}-p\cdot t$$

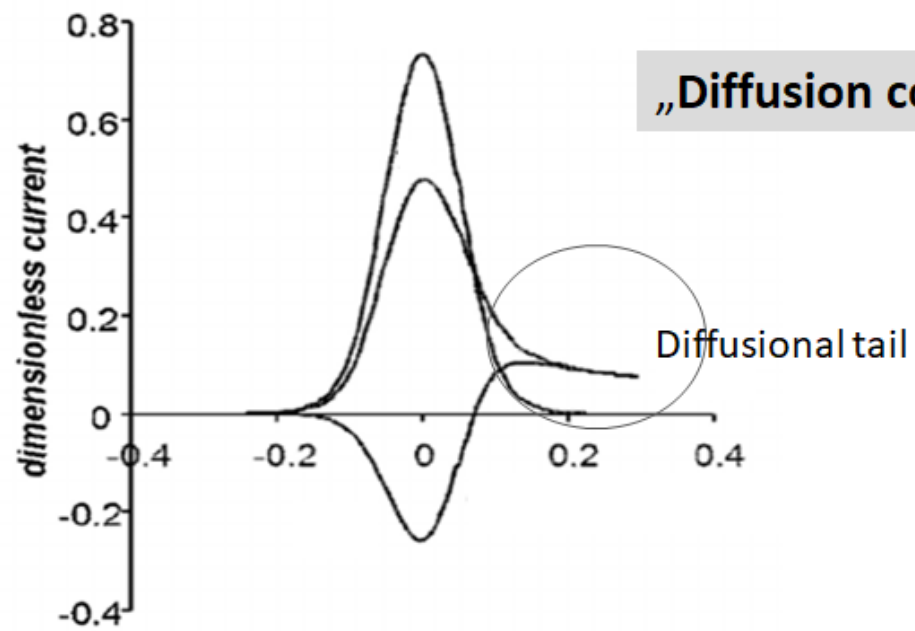


## Features of the potential ramp in SWV and the manner for current measurements in SWV

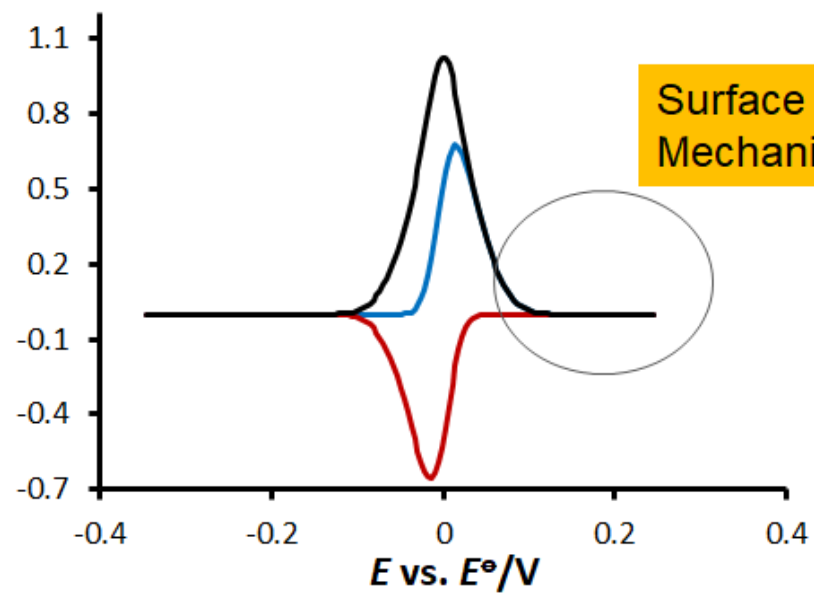




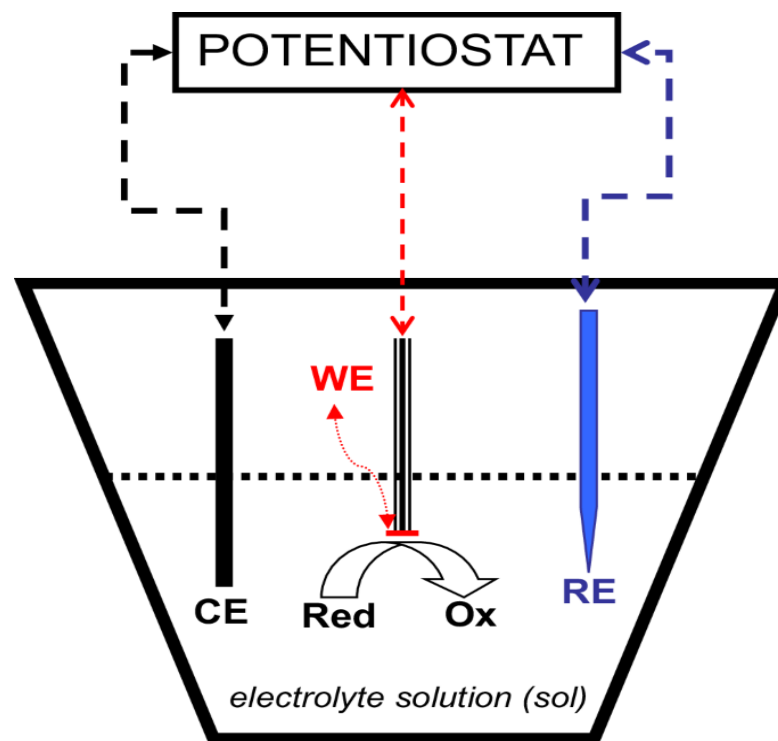
„Diffusion controlled reaction in SWV



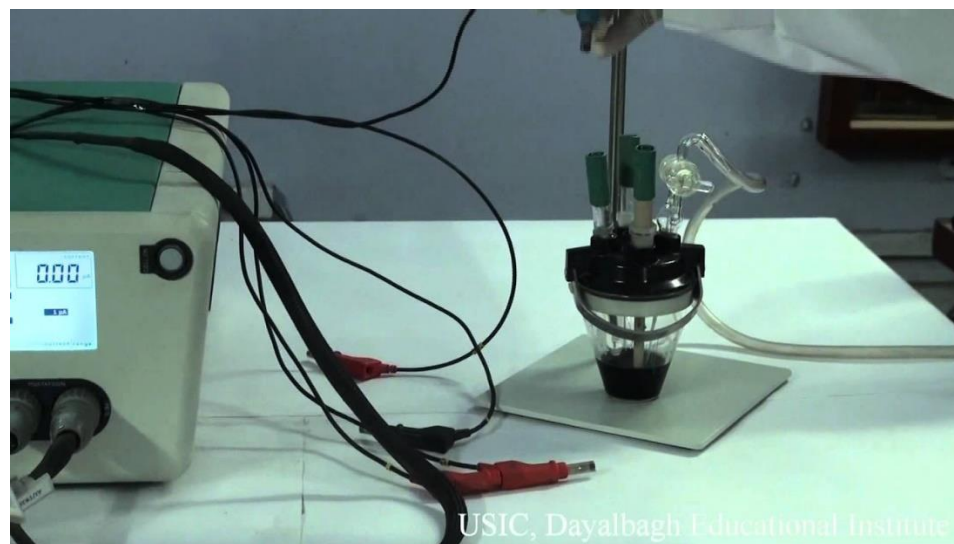
$\Psi$



Surface (adsorbed) electrode  
Mechanism in SWV



**Potentiostat and working cell used in voltammetric experiments**



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